

## Chapter End Test

Date : _____	<b>Mathematics</b>	<b>BATCH</b>
Duration: 45 Min. Max. Marks : 25	Topic : PMI & Linear Inequalities (Set-1)	<b>XI</b>

**Disclaimer:** The objective is to test the understanding of the children. For long question is to write coherently in more than one paragraph.

**General instruction:**

1. This paper consist of two Sections. Students has to attempt both sections.
2. Section – A is objective carry 1 mark each.
3. Section – B is subjective.

### [Section – A]

1. Let  $P(n)$ : " $2^n < (1 \times 2 \times 3 \times \dots \times n)$ ", then the smallest positive integer for which  $P(n)$  true is  
 (a) 1 (b) 2  
 (c) 3 (d) 4
2. A student was asked to prove a statement  $P(n)$  by induction. He proved that  $P(k + 1)$  is true whenever  $P(k)$  is true for all  $k > 5 \in \mathbb{N}$  and also that  $P(5)$  is true. On the basis of this he could conclude that  $P(n)$  is true  
 (a) for all  $n \in \mathbb{N}$  (b) for all  $n > 5$   
 (c) for all  $n \geq 5$  (d) for all  $n < 5$
3. If  $P(n)$  : " $2 \cdot 4^{2n+1} + 3^{3n+1}$  is divisible by  $\lambda$  for  $n \in \mathbb{N}$ " is true, then the value of  $\lambda$  is  
 (a) 10 (b) 11  
 (c) 12 (d) 13
4. If  $P(n)$  : " $49^n + 16^n + k$  is divisible by 64 for  $n \in \mathbb{N}$ " is true, then the value of  $k$  is  
 (a) 1 (b) 0  
 (b) -1 (d) 2
5.  $P(n)$  : " $\sqrt{n} < \frac{1}{\sqrt{1}} + \frac{1}{\sqrt{2}} + \dots + \frac{1}{\sqrt{n}}$  :  $P(n)$  is true for  
 (a)  $n \geq 2$  (b)  $n > 2$   
 (c)  $n \in \mathbb{N}$  (d)  $n < 2$
6. If  $\frac{|x-2|}{x-2} \geq 0$ , then  
 (a)  $x \in [2, \infty)$  (b)  $x \in (2, \infty)$   
 (c)  $x \in (-\infty, 2)$  (d) none of these
7. The length of a rectangle is three times the breadth. If the minimum perimeter of the rectangle is 160 cm, then  
 (a) breadth  $> 20$  cm (b) length  $< 20$  cm  
 (c) breadth  $\geq 20$  cm (d) length  $\leq 20$  cm
8. Solution of the inequalities comprising a system in variable  $x$  are represented on number lines as given below, then



- |   |                     |
|---|---------------------|
| (a) $x \in (-\infty, -4] \cup [3, \infty)$  | (b) $x \in [-3, 1]$ |
| (c) $x \in (-\infty, -4] \cup [-3, \infty)$ | (d) $x \in [-4, 3]$ |

- 9.** If  $|x + 3| \geq 10$ , then  
 (a)  $x \in (-13, 7]$  (b)  $x \in (-13, 7)$   
 (c)  $x \in (\infty, -13] \cup [7, \infty)$  (d)  $x \in (-\infty, -13] \cup [7, \infty)$
- 10.** If  $x < 5$ , then  
 (a)  $-x < -5$  (b)  $-x \leq -5$   
 (c)  $-x > -5$  (d)  $-x \geq -5$
- 11.** Given that  $x, y$  and  $b$  are real numbers and  $x < y, b < 0$ , then  
 (a)  $\frac{x}{b} < \frac{y}{b}$  (b)  $\frac{x}{b} \leq \frac{y}{b}$   
 (c)  $\frac{x}{b} > \frac{y}{b}$  (d)  $\frac{x}{b} \geq \frac{y}{b}$
- 12.** If  $-3x + 17 < -13$ , then  
 (a)  $x \in (10, \infty)$  (b)  $x \in [10, \infty)$   
 (c)  $x \in (-\infty, 10]$  (d)  $x \in [-10, 10)$
- 13.** If  $xy > 0$ , then  $x > 0$  and  $y < 0$   
 (a) True (b) False  
 (c) Can't say (d) none of these
- 14.** If  $(x - 2)^2 > 0$ , then  
 (a)  $x \in \mathbb{R}$  (b)  $x \geq 2$   
 (c)  $x > 2$  (d)  $x < 2$
- 15.** Is  $x^2 < 0$   
 (a) True (b) False  
 (c) Can't say (d) none of these

**[Section – B]**

- 16.** Using the principle of mathematical induction prove that: **[4]**

$$1^3 + 2^3 + 3^3 + \dots + n^3 = \left\{ \frac{n(n+1)}{2} \right\}^2 \text{ for } n \in \mathbb{N}.$$

- 17.** Solve the following system of inequalities: **[6]**

$$\frac{x}{2x+1} \geq \frac{1}{4}, \frac{6x}{4x-1} < \frac{1}{2}$$

**OR**

A solution of 9% acid is to be diluted by adding 3% acid solution to it. The resulting mixture is to be more than 5% but less than 7% acid. If there is 460 liters of the 9% solution, how many liters of 3% solution will have to be added?



## Hints/Solutions to Chapter End Test

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**[Section – A]**

- |         |         |
|---------|---------|
| 1. (d)  | 2. (c)  |
| 3. (b)  | 4. (c)  |
| 5. (a)  | 6. (b)  |
| 7. (c)  | 8. (d)  |
| 9. (d)  | 10. (c) |
| 11. (c) | 12. (a) |
| 13. (b) | 14. (a) |
| 15. (c) |         |

**[Section – B]**

17.  $x$  has no solution

**OR**

More than 230 liters but less than 920 liters

(230 liter  $< x < 920$  liters)

